

Summer Review Work For Students Entering Algebra 1 Honors

The attached packet is being given as a review of math topics that you should be comfortable with. These will be necessary skills for success in Algebra 1 Honors class. Your packet will be collected during the first week of school. It will be graded on completeness and correctness. After giving you an opportunity to ask questions and get clarification, you will be assessed on this content. Please use a pencil and make sure to show relevant work. You will lose points if you fail to show the required work to reach the correct answers.

Please do not wait until the last day of vacation to get started! On the other hand, do NOT attempt to complete the packet during the first week of vacation. This packet is designed to maintain your current knowledge of math concepts so that the topics discussed in the fall will be fresh in your mind.

If you have difficulties with the packet, use the examples given or feel free to search the internet for help on certain topics. Also, it may be beneficial to work with others.

Have an enjoyable summer!

I look forward to working with you this fall.

Ms. Ames

1

Basic Arithmetic

Key Terms

addition
 subtraction
 multiplication
 division
 sum
 difference
 product
 dividend
 divisor
 quotient
 remainder
 mixed operations
 bracket
 integer/whole number
 multiple

factor
 prime number
 composite number
 common multiple
 lowest common multiple
 common factor
 highest common factor
 fraction bar
 numerator
 denominator
 proper fraction
 improper fraction
 mixed fraction
 complex fraction

1.1 Four Basic Arithmetic Operations

(a) Basic operation	Example
Addition	$3 + 9 = 12$ sum
Subtraction	$13 - 5 = 8$ difference
Multiplication	$2 \times 7 = 14$ product
Division	$29 \div 6 = 4 \cdots 5$ dividend quotient remainder divisor

(b) In performing **mixed operations**, we should follow the order of operations below:

(i) Perform multiplication (\times) and division (\div) first, then addition (+) and subtraction (-).

e.g. (1) $30 - 6 \times 3$
 $= 30 - 18$
 $= \underline{12}$

(2) $5 + 14 \div 7$
 $= 5 + 2$
 $= \underline{7}$

(ii) When there are only addition / subtraction (or only multiplication / division) in an expression, perform the operations from LEFT to RIGHT.

e.g. (1) $34 - 15 + 5$
 $= 19 + 5$
 $= \underline{24}$

(2) $28 \div 4 \times 3$
 $= 7 \times 3$
 $= \underline{21}$

(iii) When there are **brackets** in an expression, perform the operations inside the brackets first.

e.g. $24 \div (4 \times 2) - 2$
 $= 24 \div 8 - 2$
 $= 3 - 2$
 $= \underline{1}$

Example 1 Calculate the following.

(a) $8 \times 2.5 - 51 \div 3$

(b) $35 \div (16 - 3 \times 2) + 1.5$

Solution (a) $8 \times 2.5 - 51 \div 3$

$= 20 - 17$

$= \underline{3}$

(b) $35 \div (16 - 3 \times 2) + 1.5$

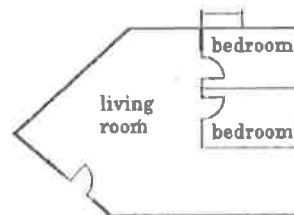
$= 35 \div (16 - 6) + 1.5$

$= 35 \div 10 + 1.5$

$= 3.5 + 1.5$

$= \underline{5}$

Example 2 In each flat of a building, there are a living room with area 50 m^2 and two bedrooms with area 10 m^2 each.



- (a) Find the total area of the flat.
 (b) If the building has 21 flats, find the sum of the areas of these flats.

Solution (a) Total area = $10 + 10 + 50$
 $= \underline{70 \text{ (m}^2\text{)}}$

(b) Sum of areas = 70×21
 $= \underline{1\,470 \text{ (m}^2\text{)}}$

Let's Try It!

Calculate the following. [Nos. 1–4]

1. $28 - 19 + 7$

=

2. $14 + 8 \times 12 - 55$

= $14 + \boxed{} - 55$

=

3. $16 - (24 - 5 \times 3)$

= $\boxed{} - (\boxed{} - \boxed{})$

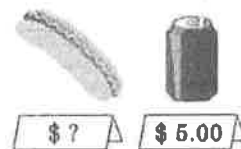
= $\boxed{} - \boxed{}$

=

4. $(8 - 5.4) \div 13 \times 2$

=

5. Mr Wong orders 3 hot dogs and 2 cans of coke in a fast food shop. The coke is sold at \$5 per can and Mr Wong pays \$46 in total. Find the price of a hot dog.



1.2 Multiples and Factors

(a) Multiples

$$\begin{aligned} 6 \times 1 &= 6 \\ 6 \times 2 &= 12 \\ 6 \times 3 &= 18 \\ &\vdots \end{aligned}$$

← Multiples of 6

∴ The first 3 multiples of 6 are 6, 12 and 18.

(b) Factors

(i) Consider the following expression.

$$8 \div 2 = 4$$

← Remainder is 0.

4 is an integer.

∴ 8 is divisible by 2.

(ii) Consider the following expression.

$$12 \div 3 = 4 \quad \leftarrow 12 \text{ is divisible by } 3.$$

∴ 3 is a **factor** of 12.

e.g. $12 = 1 \times 12$
 $= 2 \times 6$
 $= 3 \times 4$

∴ Factors of 12 are 1, 2, 3, 4, 6 and 12.

(c) Prime Numbers and Composite Numbers

(i) Numbers having only two factors (1 and itself) are called **prime numbers**.

e.g. Prime numbers up to 20 are 2, 3, 5, 7, 11, 13, 17 and 19.

(ii) Numbers having 3 or more factors (including 1) are called **composite numbers**.

e.g. Composite numbers up to 10 are 4, 6, 8, 9 and 10.

Number	Factor	Prime Numbers	Composite Numbers
1	1	×	×
2	1, 2	✓	×
3	1, 3	✓	×
4	1, 2, 4	×	✓
5	1, 5	✓	×
6	1, 2, 3, 6	×	✓



(d) Lowest Common Multiple (L.C.M.)

Multiples of 6 are 6, 12, (18), 24, 30, (36), ...

Multiples of 9 are 9, (18), 27, (36), 45, ...

The circled numbers 18 and 36 are called the **common multiples** of 6 and 9.

The smallest common multiple is called the **lowest common multiple** (abbreviated as L.C.M.).

∴ The L.C.M. of 6 and 9 is 18.

(e) Highest Common Factor (H.C.F.)

Factors of 18 are (1), (2), (3), (6), 9, 18

Factors of 24 are (1), (2), (3), 4, (6), 8, 12, 24

The circled numbers 1, 2, 3 and 6 are called the **common factors** of 18 and 24.

The largest common factor is called the **highest common factor** (abbreviated as H.C.F.).

∴ The H.C.F. of 18 and 24 is 6.

Example 3 Write down the factors of 12 and 32. Hence, find the H.C.F. of 12 and 32.

Solution Factors of 12 are 1, 2, 3, 4, 6 and 12.
Factors of 32 are 1, 2, 4, 8, 16 and 32.
∴ The H.C.F. of 12 and 32 is 4.

Example 4 Write down the first 5 multiples of 16 and 20. Hence, find the L.C.M. of 16 and 20.

Solution The first 5 multiples of 16 are 16, 32, 48, 64 and 80.
The first 5 multiples of 20 are 20, 40, 60, 80 and 100.
∴ The L.C.M. of 16 and 20 is 80.

Let's Try 1.2

1. Write down the factors of 14 and 35. Hence, find the H.C.F. of 14 and 35.

Solution Factors of 14 are _____, _____, _____, _____.

Factors of 35 are _____, _____, _____, _____.

∴ The H.C.F. of 14 and 35 is _____.

2. Write down the first 5 multiples of 8 and 10. Hence, find the L.C.M. of 8 and 10.

Solution The first 5 multiples of 8 are _____.

The first 5 multiples of 10 are _____.

∴ The L.C.M. of 8 and 10 is _____.

3. Write down all the prime numbers from 20 to 30.

Solution The prime numbers from 20 to 30 are _____.

1.3 Fractions

(a) Types of Fractions

fraction bar \longrightarrow $\frac{3}{5}$ \longleftarrow numerator
 \longleftarrow denominator

The following are 3 common types of fractions:

Type	Meaning	Example
Proper fraction	a fraction with a numerator less than the denominator	$\frac{1}{4}, \frac{2}{7}, \frac{8}{15}$
Improper fraction	a fraction with a numerator greater than or equal to the denominator	$\frac{7}{7}, \frac{11}{6}, \frac{10}{4}$
Mixed fraction	a sum of a natural number and a proper fraction	$1\frac{2}{7}, 3\frac{1}{5}, 12\frac{3}{8}$

Note: In a fraction, if the numerator, denominator or both contain a fraction, the fraction is called a **complex fraction**.

$$\frac{\frac{3}{5}}{\frac{9}{10}}$$

is a complex fraction and $\frac{\frac{3}{5}}{\frac{9}{10}} = \frac{3}{5} \div \frac{9}{10}$

(b) Operations with Fractions

(i) Addition or subtraction:

Expand the fractions to make their denominators the same first, then add or subtract the numerators.

Example 5 Calculate $\frac{1}{2} - \frac{2}{7}$.

Solution

$$\begin{aligned} & \frac{1}{2} - \frac{2}{7} \\ &= \frac{7-4}{14} \\ &= \underline{\underline{\frac{3}{14}}} \end{aligned}$$

The L.C.M. of 2 and 7 is 14.

$$\therefore \frac{1}{2} = \frac{1 \times 7}{2 \times 7} = \frac{7}{14}$$

$$\frac{2}{7} = \frac{2 \times 2}{7 \times 2} = \frac{4}{14}$$

(ii) Multiplication or division:

Convert all mixed fractions into improper fractions first, then cancel out all the common factors in the numerators and the denominators.

Example 6 Calculate the following.

(a) $\frac{\frac{2}{3}}{\frac{4}{9}}$

(b) $\frac{1}{6} \times \frac{3}{4} + \frac{5}{6} \div 1\frac{1}{3}$

Solution

(a) $\frac{\frac{2}{3}}{\frac{4}{9}}$

$$\begin{aligned} &= \frac{2}{3} \div \frac{4}{9} \\ &= \frac{2}{3} \times \frac{9}{4} \\ &= \frac{3}{2} \\ &= \underline{\underline{1\frac{1}{2}}} \end{aligned}$$

To divide a fraction by another, turn the divisor upside down and convert ' \div ' into ' \times '.

$$\begin{aligned}
 \text{(b)} \quad & \frac{1}{6} \times \frac{3}{4} + \frac{5}{6} \div 1\frac{1}{3} \\
 & = \frac{1}{6} \times \frac{3}{4} + \frac{5}{6} \div \frac{4}{3} \\
 & = \frac{1}{6} \times \frac{3}{4} + \frac{5}{6} \times \frac{3}{4} \\
 & = \frac{1}{8} + \frac{5}{8} \\
 & = \frac{6}{8} \\
 & = \frac{3}{4}
 \end{aligned}$$

Convert into improper fraction first.

Simplify the answer.
 $\frac{6}{8}$

Let's Try 1.3

Calculate the following.

1. $\frac{4}{9} + \frac{5}{12}$

$$= \frac{\boxed{}}{\boxed{}}$$

=

2. $2\frac{4}{7} - 1\frac{1}{3}$

=

3. $2\frac{5}{8} \times 1\frac{2}{7}$

=

4. $\frac{2}{5} = \frac{2}{5} \div \boxed{}$

=

5. $1 - 1\frac{1}{5} \div 12$

$$= 1 - \boxed{} \times \boxed{}$$

$$= 1 - \boxed{}$$

=

6. $\frac{7}{9} \times 3 + 3\frac{1}{2} \div 14$

$$= \frac{7}{9} \times 3 + \boxed{} \times \boxed{}$$

$$= \boxed{} + \boxed{}$$

=

Exercise 1

Calculate the following. [Nos. 1–8]

1. $15 \times 5 \div 3$
=

2. $2.5 - 1.4 + 3 \times 0.3$
=

3. $50 - 9.2 \times 5 + 13$
=

4. $(5.2 + 4.3) \div 5$
=

5. $\frac{\frac{3}{7}}{\frac{5}{21}}$
=

6. $(2\frac{1}{2} - 3 \times \frac{2}{3}) \div \frac{1}{2}$
=

7. $(8\frac{2}{7} - 4\frac{1}{5} \times \frac{10}{7}) \div \frac{7}{12}$
=

8. $3\frac{1}{2} \times (2\frac{1}{2} + \frac{5}{6}) \div (\frac{1}{6} \times \frac{1}{3})$
=

9. Write down the factors of 15 and 30. Hence, find the H.C.F. of 15 and 30.

Solution Factors of 15 are _____,

Factors of 30 are _____

∴ The H.C.F. of 15 and 30 is _____

10. Write down the first 8 multiples of 12 and 28. Hence, find the L.C.M. of 12 and 28.

Solution The first 8 multiples of 12 are _____

The first 8 multiples of 28 are _____

∴ The L.C.M. of 12 and 28 is _____

11. Write down all the composite numbers from 31 to 59.

Solution Composite numbers from 31 to 59 are _____

Fill in the \square with '+', '-', '×' or '÷' to make the both sides of the following expressions equal. [Nos. 12–13]

12. $\frac{1}{11} \square 8 \square \frac{10}{11} \times \frac{1}{8} = \frac{1}{8}$

13. $\left(\frac{1}{2} \square \frac{1}{3} + \frac{1}{6}\right) \square 36 = 12$

14. Taxi Fare Table

First 2 km	\$22.00
Every subsequent 0.2 km	\$1.60
Every piece of baggage	\$5.00

City A and city B are 4 km apart. City B and city C are 13.2 km apart. Paco took a taxi from A to C via B without any baggage. How much taxi fare should he pay?



Basic Skills Practice

Using Ratios and Rates, Part 1

A ratio is a comparison of two numbers or quantities. Ratios may be written three different ways:

$$\frac{2}{7} \quad 2 \text{ to } 7 \quad 2 : 7$$

Ratios can be used to make predictions.

Example 1: Arthur makes 2 goals for every 7 attempts. Predict how many goals will he make in 35 attempts.

Compare: $\frac{\text{goals}}{\text{attempts}} = \frac{2}{7}$

Make equivalent ratios. (Making equivalent ratios is like making equivalent fractions.)

Goals	2	4	6	8	10
Attempts	7	14	21	28	35

We can expect Arthur to make 10 goals in 35 attempts.

Ratios can be used to determine how many times greater one number is than another.

Example 2: Richard is 16 years old. Martha is 4 years old. How many times older is Richard than Martha?

Compare: $\frac{\text{Richard's age}}{\text{Martha's age}} = \frac{16}{4}$ Divide: $\frac{16}{4} = 4$

Richard is 4 times older than Martha.

Ratios can be used to compare amounts when the units of measure are the same.

Example 3: A punch recipe uses 4 cups of water and 16 ounces of orange concentrate. What is the ratio of water to concentrate?

Make sure the units are the same. Change 16 ounces to 2 cups.

Compare: $\frac{\text{water}}{\text{concentrate}} = \frac{4 \text{ cups}}{2 \text{ cups}} = \frac{2 \text{ cups}}{1 \text{ cup}}$

The ratio of water to concentrate is 2 cups of water to 1 cup of concentrate.

A ratio that compares two different kinds of quantities is called a rate.

Examples of rates: $\frac{\text{miles}}{\text{hour}}$, $\frac{\text{miles}}{\text{gallon}}$

When the rate has a denominator of 1, it is called a unit rate.

Example 4: A car travels 300 miles on 12 gallons of gasoline. What is the unit rate in miles per gallon (mpg)?

A unit rate compares a quantity to a unit of one.

Compare: $\frac{\text{miles}}{\text{gallons}} = \frac{300}{12} = 25 \text{ mpg}$

Write three equivalent ratios for each given ratio.

1. $\frac{5}{6}$ _____

2. $\frac{2}{3}$ _____

Write a ratio that compares each quantity.

3. the number of vowels to the number of consonants in the alphabet _____

4. the number of months that end in y to the total number of months in a year _____



Basic Skills Practice

Using Proportions, Part 1

A proportion is an equation stating that two ratios are equal.

$$1:2 \text{ and } 4:8 \text{ form the proportion } \frac{1}{2} = \frac{4}{8}$$

Cross products can be used to tell if two ratios form a proportion.

$$\frac{1}{2} = \frac{4}{8} \quad 2 \times 4 = 8 \quad 1 \times 8 = 8 \quad \text{Yes} \quad \frac{1}{3} = \frac{4}{5} \quad 3 \times 4 = 12 \quad 1 \times 5 = 5 \quad \text{No}$$

Cross products can be used to find the missing term in a proportion. $\frac{18}{n} = \frac{6}{3}$

Example 1: Find the value of n in $\frac{18}{n} = \frac{6}{3}$.

$$\begin{aligned} \text{Use cross products: } 6 \times n &= 18 \times 3 \\ 6n &= 54 \\ n &= 9 \end{aligned}$$

Proportions can help solve problems.

Example 2: What is the cost of a dozen oranges if 3 oranges cost 99 cents?

$$\begin{aligned} \frac{3}{99} &= \frac{12}{n} \\ 3n &= 1188 \\ n &= 396 \end{aligned}$$

12 oranges cost 396 cents or \$3.96

Does each pair of ratios form a proportion? Write yes or no.

1. $\frac{3}{9}, \frac{6}{18}$ _____

2. $\frac{9}{10}, \frac{18}{30}$ _____

3. $\frac{1}{2}, \frac{50}{100}$ _____

4. $\frac{10}{20}, \frac{30}{40}$ _____

5. $\frac{55}{121}, \frac{5}{11}$ _____

6. $\frac{0.4}{2.3}, \frac{1.6}{9.2}$ _____

Solve each equation for n .

7. $\frac{48}{n} = \frac{4}{7}$ _____

8. $\frac{9}{24} = \frac{n}{48}$ _____

9. $\frac{4}{18} = \frac{6}{n}$ _____

10. $\frac{n}{55} = \frac{18}{22}$ _____

11. $\frac{5.1}{n} = \frac{1.7}{2}$ _____

12. $\frac{16}{34} = \frac{n}{1.7}$ _____

Solve by using a proportion.

13. Joe's favorite flavor of frozen yogurt is chocolate fudge. There are 65 calories in 2 ounces of chocolate fudge frozen yogurt. How many calories are there in 10 ounces? _____

14. One roll of gift wrap will wrap 4 shirt boxes. How many rolls will be needed to wrap 24 shirt boxes? _____

15. Elissa drives 164 miles in 4 hours. At that rate, how many miles will she travel in 6.5 hours? _____



Basic Skills Practice

Similar Figures, Part 1

Two or more figures that have the same shape but different sizes are called *similar figures*. Triangle ABC and triangle DEF are similar figures. This is written as $\triangle ABC \sim \triangle DEF$.

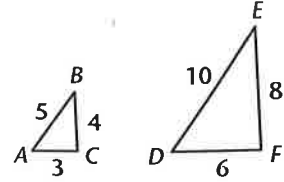
When two figures are similar,

- the corresponding angles are congruent.

$$\angle A \cong \angle D \quad \angle B \cong \angle E \quad \angle C \cong \angle F$$

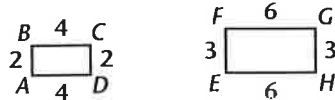
- the ratios of the lengths of the corresponding sides are equal.

$$\frac{AB}{DE} = \frac{5}{10} = \frac{1}{2} \quad \frac{BC}{EF} = \frac{4}{8} = \frac{1}{2} \quad \frac{AC}{DF} = \frac{3}{6} = \frac{1}{2}$$



You can determine if two figures are similar by checking to see that they meet both conditions:

Example 1: Are rectangle $ABCD$ and rectangle $EFGH$ similar?



- Because both figures are rectangles, all angles are right angles, so they are all congruent.

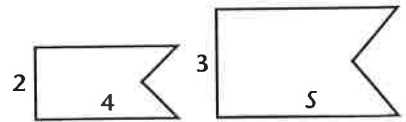
$$\frac{AB}{EF} = \frac{2}{3} \quad \frac{BC}{FG} = \frac{4}{6} = \frac{2}{3} \quad \frac{CD}{GH} = \frac{2}{3} \quad \frac{DA}{HE} = \frac{4}{6} = \frac{2}{3}$$

The ratios of the corresponding sides are equal, so rectangle $ABCD \sim$ rectangle $EFGH$.

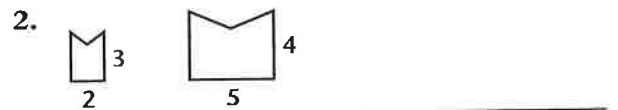
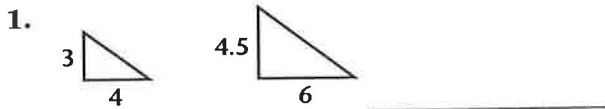
You can find the length of the missing side in similar figures by using proportions.

Example 2: The two flags are similar. What is the length of s ?

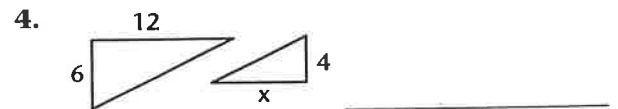
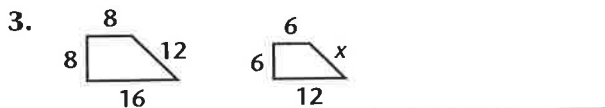
Write a proportion. $\rightarrow \frac{2}{3} = \frac{4}{s}$
 Solve the proportion. $\rightarrow 2s = 12$
 $s = 6$



Determine if the pairs of figures are similar. Write *yes* or *no* in the blank spaces.



Each pair of figures is similar. Find the length of the missing side.



6

Perimeter, Area and Volume

Key Terms

length

width/breadth

base

height

upper base

lower base

splitting method

filling method

capacity

container

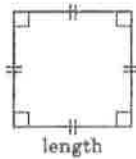
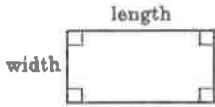
dimensions

depth

maximum

6.1 Perimeters of Simple Plane Figures

(a) Perimeter of a plane figure = sum of the lengths of all its sides

<i>Plane figure</i>	<i>Perimeter</i>
 <p>length</p>	Perimeter of a square = length \times 4
 <p>length</p> <p>width</p>	Perimeter of a rectangle = (length + width) \times 2

(b) mm, cm, m and km are common measuring units of lengths.

Example 1 The figure shows a rectangle formed by 3 squares with side 8 cm. Find the perimeter of the rectangle.



Solution Length of the rectangle = 8×3
 $= 24$ (cm)

\therefore Perimeter of the rectangle = $(24 + 8) \times 2$
 $= \underline{64}$ (cm)

Example 2 Andy uses a wire of 48 mm long to form a square.
Find the length of the square.

48 mm



Solution Let x mm be the length of the square.

$$4x = 48$$

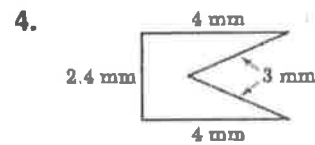
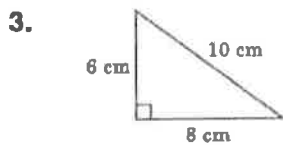
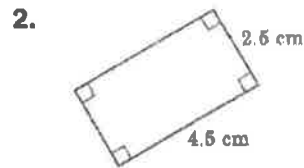
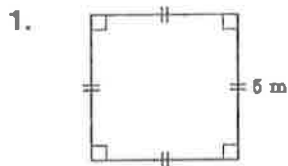
$$\frac{4x}{4} = \frac{48}{4}$$

$$x = 12$$

\therefore The length of the square is 12 mm.

Let's Try 6.1

Find the perimeters of the following figures. [Nos. 1–4]




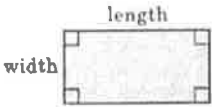
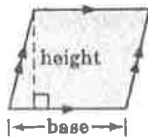
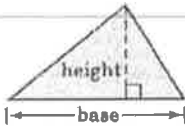
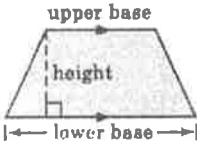
5. The perimeter of a rectangle is 110 cm. If the length is 42 cm, find the width.

Solution Let y cm be the width.

$$(\square + \square) \times \square = \square$$

\therefore The width is cm.

6.2 Areas of Simple Plane Figures

(a)	Plane figure	Area
		Area of a square = length \times length
		Area of a rectangle = length \times width
		Area of a parallelogram = base \times height
		Area of a triangle = $\frac{1}{2} \times$ base \times height
		Area of a trapezium = $\frac{1}{2} \times$ (upper base + lower base) \times height

(b) mm^2 , cm^2 , m^2 and km^2 are common measuring units of areas.

Example 3 The polygon on the right is formed by a parallelogram and a triangle. Find the area of the polygon.

Solution

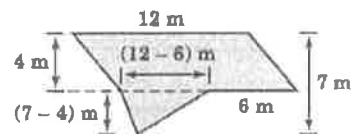
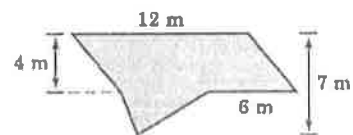
$$\begin{aligned} \text{Area of the parallelogram} &= 12 \times 4 \\ &= 48 \text{ (m}^2\text{)} \end{aligned}$$

$$\begin{aligned} \text{Area of the triangle} \\ &= \frac{1}{2} \times (12 - 6) \times (7 - 4) \end{aligned}$$

$$= \frac{1}{2} \times 6 \times 3$$

$$= 9 \text{ (m}^2\text{)}$$

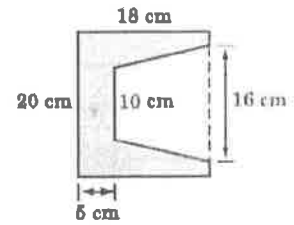
$$\therefore \text{Area of the polygon} = 48 + 9 = \underline{57 \text{ (m}^2\text{)}}$$



This is called the *splitting method*.



Example 4 In the figure, John cuts out a trapezium from a piece of rectangular paper. What is the area of the remaining part?



Solution

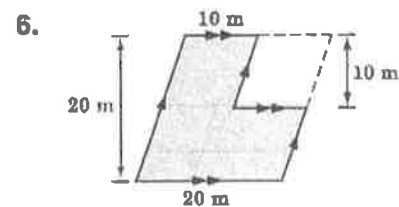
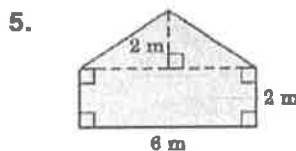
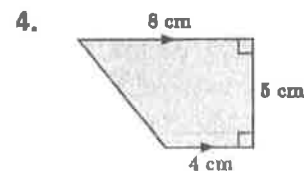
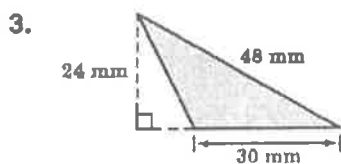
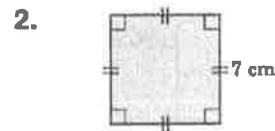
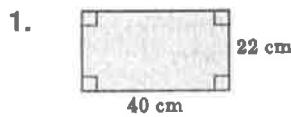
$$\begin{aligned} \text{Area of the rectangle} &= 20 \times 18 \\ &= 360 \text{ (cm}^2\text{)} \\ \text{Area of the trapezium} &= \frac{1}{2} \times (10 + 16) \times (18 - 5) \\ &= \frac{1}{2} \times 26 \times 13 \\ &= 169 \text{ (cm}^2\text{)} \\ \therefore \text{Area of the remaining part} &= 360 - 169 \\ &= \underline{\underline{191 \text{ (cm}^2\text{)}}} \end{aligned}$$

This is called the filling method.

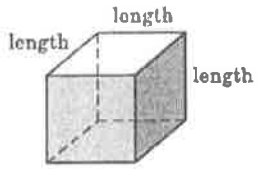
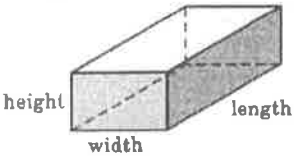


Let's Try 6.2

Find the areas of the following figures.



6.3 Volumes of Simple Solid Figures

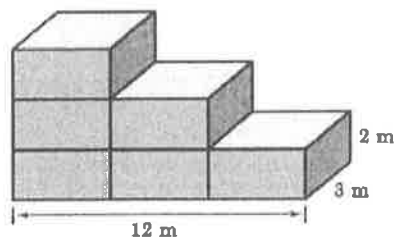
(a) <i>Solid figure</i>	<i>Volume</i>
	Volume of a cube = length \times length \times length
	Volume of a cuboid = length \times width \times height

(b) mm^3 , cm^3 , m^3 and km^3 are common measuring units of volumes. For the **capacity** of a **container** or volume of liquid, the units mL and L can also be used.

$$\begin{aligned} 1 \text{ mL} &= 1 \text{ cm}^3 \\ 1 \text{ L} &= 1\,000 \text{ cm}^3 \end{aligned}$$



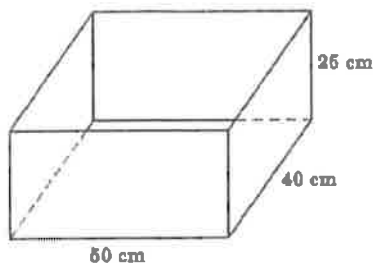
Example 5 The solid below is formed by 6 cuboids of the same size. Find the volume of the solid.



Solution

$$\begin{aligned} \text{Length of each cuboid} &= 12 \div 3 \\ &= 4 \text{ (m)} \\ \text{Volume of each cuboid} &= 4 \times 3 \times 2 \\ &= 24 \text{ (m}^3\text{)} \\ \therefore \text{Volume of the solid} &= 24 \times 6 \\ &= \underline{\underline{144 \text{ (m}^3\text{)}}} \end{aligned}$$

Example 6 The **dimensions** of the container below are 50 cm × 40 cm × 25 cm. If Dick pours 30 L of water into the container, find the **depth** of water in the container.



Solution Let d cm be the depth of water in the container.

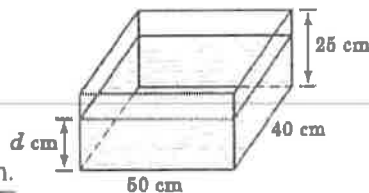
$$50 \times 40 \times d = 30 \times 1\,000 \quad \leftarrow 30 \text{ L} = 30 \times 1\,000 \text{ cm}^3$$

$$2\,000d = 30\,000$$

$$\frac{2\,000d}{2\,000} = \frac{30\,000}{2\,000}$$

$$d = 15$$

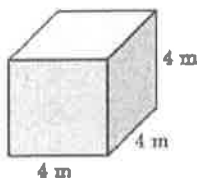
∴ The depth of water in the container is 15 cm.



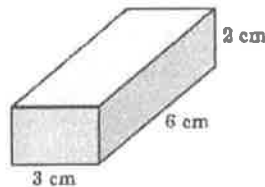
Let's Try 6.3

Find the volumes of the following solids. [Nos. 1–2]

1.

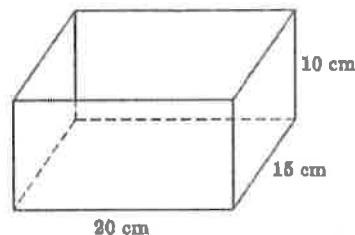


2.



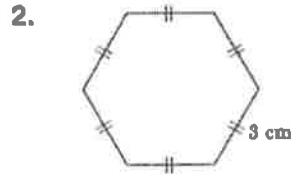
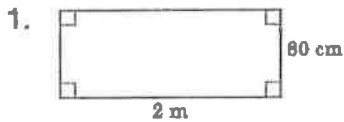
3. (a) In the figure, the capacity of the container is _____ L.

(b) Pansy pours a bottle of 1.5 L orange juice into the container. The depth of orange juice in the container is _____ cm.



Exercise 6

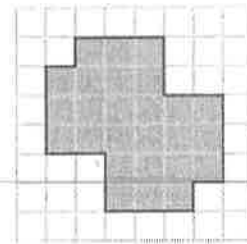
Find the perimeters of the following figures. [Nos. 1–2]



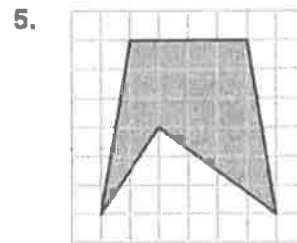
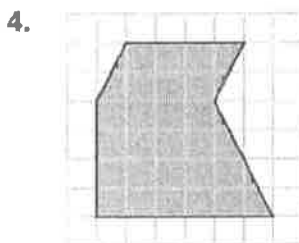
3. In the figure, the length of each small square is 1 cm.

(a) Perimeter of the shaded region is _____ cm.

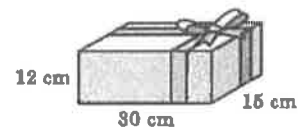
(b) Area of the shaded region is _____ cm^2 .



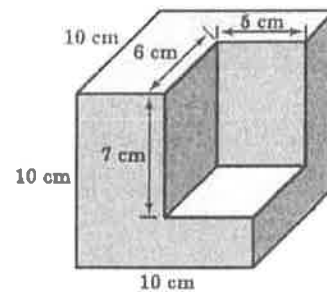
In the following figures, the length of each small square is 1 cm. Find the areas of the shaded regions. [Nos. 4–5]



6. The volume of the gift box on the right is _____ cm^3 .

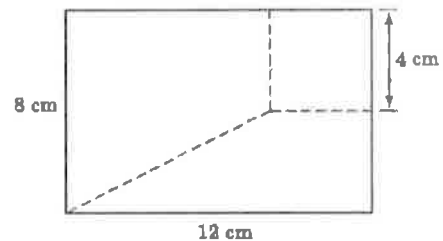


7. The figure shows the remaining part of a cube after a cuboid is cut out. The volume of this remaining part is _____ cm^3 .



8. David gives a box of candies to Mandy. The box is a cuboid with length 10 cm, width 6 cm and volume 180 cm^3 . Find the height of the box.
9. A fence of 200 m is built around a rectangular garden. If the length of the garden is 60 m, find the area of the garden.
10. Jack uses a piece of wire to form an equilateral triangle of side 14 cm. Then, Michelle reforms it to a square. What is the area of the square?

11. The figure shows a rectangle with length 12 cm and width 8 cm. It is cut into one square and two trapeziums of different sizes. If the side of the square is 4 cm, what is the area of the smaller trapezium?



12. There is a box with length 20 cm, width 12 cm and height 10 cm. Find the **maximum** number of blocks as shown on the right can be put into the box.

